

# MAPPING LARGE COMBINATIONAL CIRCUITS WITH K-LUT BASED FPGAS USING HOMOGENOUS DOMINATING CONES

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**Abstract:** *Partitioning is a technique of dividing a circuit or system into a collection of smaller blocks (sub-circuits) with roughly equal sizes targeting to minimize the number of interconnections between the blocks. Due to the limited mapping resource of k-LUT FPGAs, large combinational circuits partitioning is of practical importance for k-LUT based FPGA circuit implementation. In this paper is presented multilevel multi-resource partitioning algorithm for partitioning large combinational circuits in order to efficiently use existing and commercially available FPGAs packages.*

**Keywords:** *critical path, bottom-up clusters, top-down min-cut, homogenous dominating cones;*

## 1. INTRODUCTION

Circuit partitioning has multiple applications in VLSI design. One of the most common is that of dividing combinational circuits (usually large ones) that will not fit on a single package among a number of packages. Partitioning is of practical importance for k-LUT based FPGA circuit implementation. Partitioning is a technique of dividing a circuit or system into a collection of smaller blocks (sub-circuits) with roughly equal sizes targeting to minimize the number of interconnections between the blocks. It is, on the one hand, a design task to break a large system into pieces to be implemented on

separate interacting components and, on the other hand, it serves as an algorithmic method to solve difficult and complex combinatorial optimization problems as in logic or layout synthesis. Partitioning has been an active area of research for at least a quarter of a century [1], [2], [3], [4], [5] and [27].

The main reason that partitioning has become a central and sometimes-critical design task today is the enormous increase of system complexity in the past and the expected further advances of microelectronic system design and fabrication. Soaring system complexities result from a combination of reasons:

- Increasing circuits complexity and
- Shorter turn-around time to reach the market with new products.

Broadly accepted powerful high-level synthesis tools allow the designers to automatically generate huge systems. In a functional specification, by just changing a few lines of code, the size of the resulting structural description (net list) of a system can increase dramatically.

Synthesis and simulation EDA tools often hardly cope with the complexity of the whole system under design, and engineer aim is to concentrate on critical parts of a system in order to speed-up design cycle. It results that the present state of design technology often requires a partitioning of the system [1], [2], and [3].

Fabrication technology makes increasingly smaller feature sizes and augmented die dimensions possible, thus allowing a circuit to accommodate huge number of transistors. However, circuits are restricted in size and in the number of external I/O connections. FPGAs devices are an appropriate example [3], and [5].

Fabrication technology, obviously, requires the partitioning of a system into components. Economical pressure yields larger systems, both to make production cheaper and to exploit the optimization potential of the complete system.

The various parts of the system should be implemented in appropriate ways to achieve low-cost fabrication, optimal system performance, and easy adaptation to changing requirements, e.g. Thus, profit can be received by partitioning a system optimally [5], [6], [8], and [9].

Partitioning applications exist on all levels of abstraction, specifically on the functional (behavioral) and on the structural (net list) level. In the early stages of design, far-reaching decisions have to be made how to partition a design, often based on incomplete knowledge.

It has been observed that structure synthesis tools, in general, do not generate a hierarchy that can be used directly for mapping (FPGAs case) or for layout design if this hierarchy is deep [9], and [10]. To give the mapping and layout synthesis tools the freedom they require generating good results; net lists have to be

flattened out and repartitioned [9], [12], and [13].

In particular, it has to be decided whether to implement a component in various types of hardware technologies to achieve an optimal size/performance trade-off.

Because the granularity is low in such situation, i.e. relatively few objects of moderate to high complexities, human designers based on their experience can possibly do partitioning [5], [6], [7], and [9].

The components resulting from system partitioning are implemented by a team of designers or synthesized from a high-level description by using synthesis tools that generate a structural implementation [2], [4], and [9].

Field Programmable Gate Arrays (FPGAs), providing both large-scale integration and user-programmability, are important circuit architectures. These features have enormous impact on reducing integrated circuit manufacturing time and costs. FPGA packages, as a general feature, have maximum size CLBs constraints much larger than the number of input-output pins IOBs.

Thus, implementation of a large logic network into working FPGA involves network partitioning into a near balanced packing of Combinational Logic Blocks (CLBs) and Input-Output Blocks (IOBs). Resulting IOBs bottleneck during circuit partitioning could involve more required devices and possibly more ordinary signal wires crossing between packages. It implies more critical timing paths between packages and drastically decreases frequency operational of the circuits. Critical paths are long combinational path between sequential elements and IOBs.

Cutting critical paths during circuit partitioning into separate packages implies capacitances of packages interconnections that could drastically reduce network speed [6], [9], [12], [13], [12], [13], [14], and [15].

FPGA circuit implementation has two main phases. Placement phase, the first one, is dedicated to assign desirable locations within the FPGA structure, to the optimal system performance, and easy adaptation to changing

requirements, e.g. Thus, profit can be received by partitioning a system optimally.

Routing phase, the last one, provides the interconnections between these blocks [7], [20], [21], [22], [23], [24], [25], and [26].

Circuit partitioning is used, however, twice in FPGA implementation. First usage concerns too large designs to fit available FPGA packages. A less obvious usage of network partitioning is used in the blocks placement phase, [23], [24], [25], and [31]. Placement algorithms based on circuit partitioning yields astonishing results efficiently.

## 2. PREVIOUS RESULTS

Typical partitioning objectives such as minimum-width bisection and minimum ratio cut are NP-complete and require such heuristics as simulated annealing, greedy  $k$ -opt interchange or quadratic optimization (via relaxation or spectral methods).

Hopefully these heuristics are computing fine solution close enough to the optimal one.

The objective of two-way partitioning, [1], [2], and [3], is to either minimize the cut-size when partitioning the network into two (roughly) equal-size blocks, or to minimize the ratio cut size between the two blocks, [27].

The two-way partitioning algorithms include the Kernighan-Lin successful heuristic and iterative improvement methods, [1], [2], and [4], the graph spectrum method, [21], and the net-based partitioning method, [22].

The multi-way partitioning algorithms include the recursive Kernighan-Lin two-way partitioning method, a generalization of the spectrum-based partitioning method, [9], the generalization of the FM-algorithm with look-ahead scheme, [16], and [3].

Most recent years a number of new thoughts have been introduced supplementary improving the quality of partitioning solutions, including communication-complexity based partitioning [5], cluster-based partitioning methods, [16], and partitioning with module replication, [22], and [25].

## 3. PROBLEM FORMULATION

In this paper, is studied the partitioning problem for combinational Boolean networks. A combinational Boolean network  $C$  can be represented as a directed acyclic graph  $G = (V, E)$  where each node  $n$  ( $n \in V$ ) represents a logic gate and a directed edge  $(i, j)$ ,  $((i, j) \in E)$  exists if the output of gate  $i$  is an input of gate  $j$ .

A primary input (PI) node has no incoming edge and a primary output (PO) node has no outgoing edge. A *disjoint  $Q$ -way partitioning solution*  $S = (A_1, A_2, \dots, A_K)$  satisfies the following conditions:

- (i)  $A_i \cap A_j = \emptyset$  for  $i \neq j$  and
- (ii)  $\cup A_i$ ,  $0 < i < Q+1$ , contains all the gates in the network;

$A_1, A_2, \dots, A_K$  are known as *clusters of  $G$*  ( $C$ ).

Each node in  $C$  has only one output line and limited number of input lines. It is used  $input(v)$  to denote the set of fanins of gate.

Given a subgraph  $H$  of the Boolean network, let  $input(H)$  denote the set of *distinct* nodes outside  $H$ , which supply inputs to the nodes in  $H$  (*fanins of  $H$* ). For a node  $n$  in the network, a *w-feasible cone at  $n$* , denoted  $K_n$ , is a subgraph consisting of node  $n$  and its predecessors ( $u$  is a predecessor of  $n$  if there is a directed path from  $u$  to  $n$ ), such that  $|input(K_n)| \leq w$  and any path connecting a node in  $K_n$  and  $n$  lies entirely in  $K_n$ .

The *level* of a node is the length of the longest path from any PI node to  $n$ . The level of a PI node is zero.

The *depth* of a network is the *largest node level* in the network.

A Boolean network is *p-bounded* if  $|input(n)| \leq p$  for each node  $n$  in the network.

Since it is always attractive having disjoint partitioning solutions, the word 'disjoint' might be omitted in later discussions.

Main objective is to minimize the total number of nets between different partitions.

Moreover, for a multi-way partitioning solution  $S$ , one can define a directed graph  $D(S)$ , called the *dependency graph* of  $S$ , such that each node in  $D(S)$  represents a block in  $S$ , and there is a directed edge  $(A_i, A_j)$  in  $D(S)$  if and only if there exists an edge  $(x, y)$  in  $C$  such that  $x \in A_i$  and  $y \in A_j$ .

The assumption that it is given a combinational

network guarantees the existence of disjoint partitioning solution.

When it is given a general net list, one can first remove all the sequential elements in order to obtain only a combinational network, [15], [23], and [24].

Most of existing partitioning methods model a network as an undirected graph or hyper graph, and ignore the signal directions during the partitioning process.

However, the study in this paper shows that considering signal directions is very helpful in identifying the underlining circuit structure, which can lead to significant improvement on the partitioning results.

#### 4. CLUSTER PARTITIONING ALGORITHM

Cluster partitioning algorithm was implemented using SIS-1.2 structures and routines and most of the terminology used in this paper is similar to the terminology used in SIS-1.2 documentation.

Implemented algorithm split-up C using directed acyclic graph  $G$  (as model of this combinational Boolean network), before mapping  $K$ -LUT nodes in the circuit.

Combinational circuits could be very large and cluster partitioning helps obtaining more technological compliant mapping over the initial circuit.

Before starting the first network traversal, all nodes are inserted in a partial-ordered structure, such that each node  $n_i$  feeding node  $n_j$  appears before  $n_j$  in this structure.

Each internal node structure has an additional array denoted  $po\_label$ , mapping all POs nodes of the circuit; ( $po\_label(\beta)$  is mapping  $PO_\beta$ , as an example). This array it's initialized with zero.

First traversal, depth first search from outputs, establish nodes affiliation with respect to the *primary output nodes*. Primary output nodes in figure 1 are  $z$ ,  $x$ ,  $y$ , and  $w$ .

An internal node having more than one element not zero in its  $po\_label$  belongs to more than one primary output transitive cone, and it's said to be *multiple dominated*.

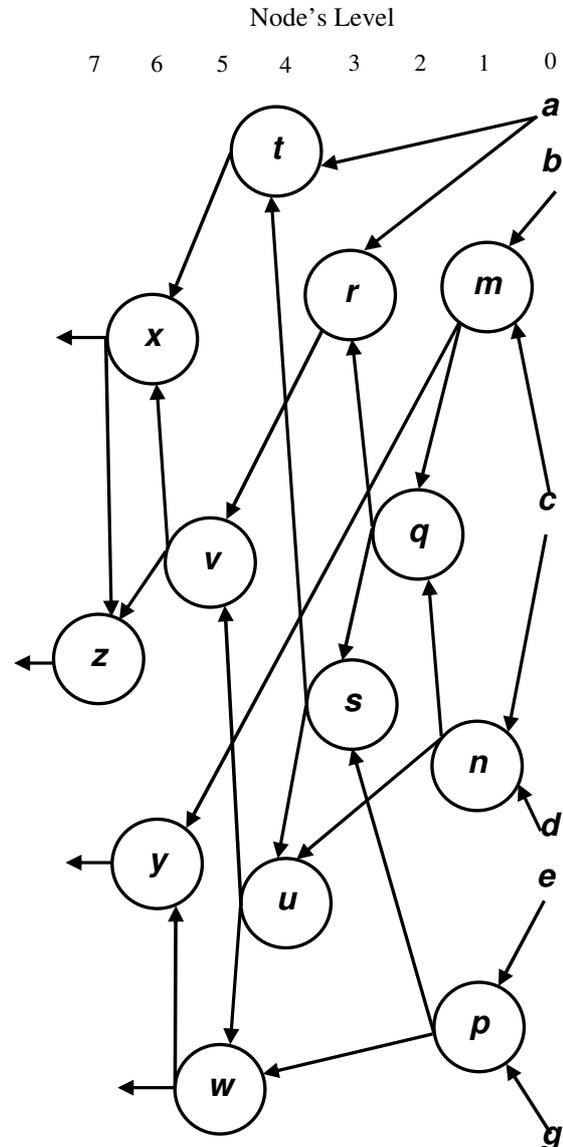
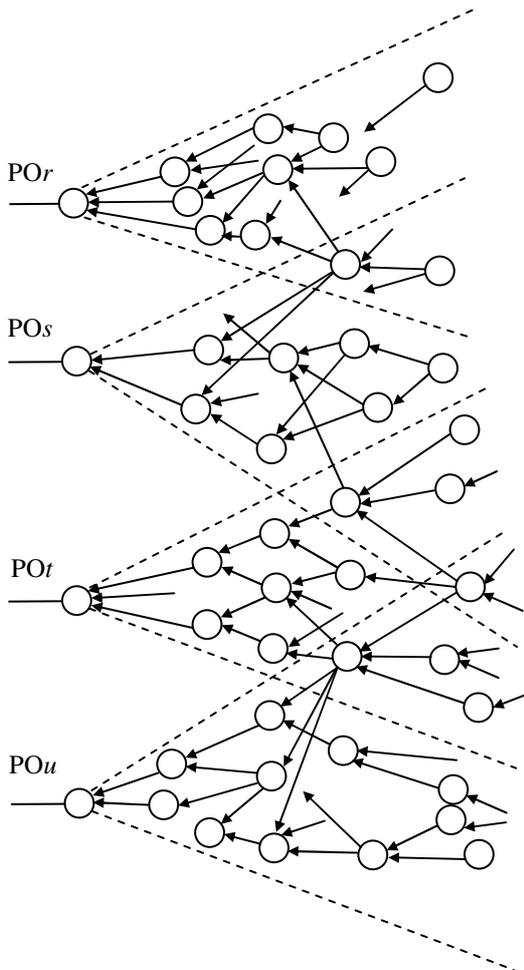


Fig. 1. Directed acyclic graph representing multilevel combinational circuit.

If node  $n$  belongs to the transitive cones of  $PO_1$ ,  $PO_2$  and  $PO_3$ , as an example, then  $po\_label(1) = po\_label(2) = po\_label(3) = 1$ . All such nodes are defining sub-cone(1,2,3) as the intersection of the three mentioned cones.

Node  $t$ , in figure 1, has  $po\_label$  marking  $w$ ,  $x$ ,  $y$ , and  $z$  affiliation, while primary output node  $w$  has affiliated only node  $y$ .



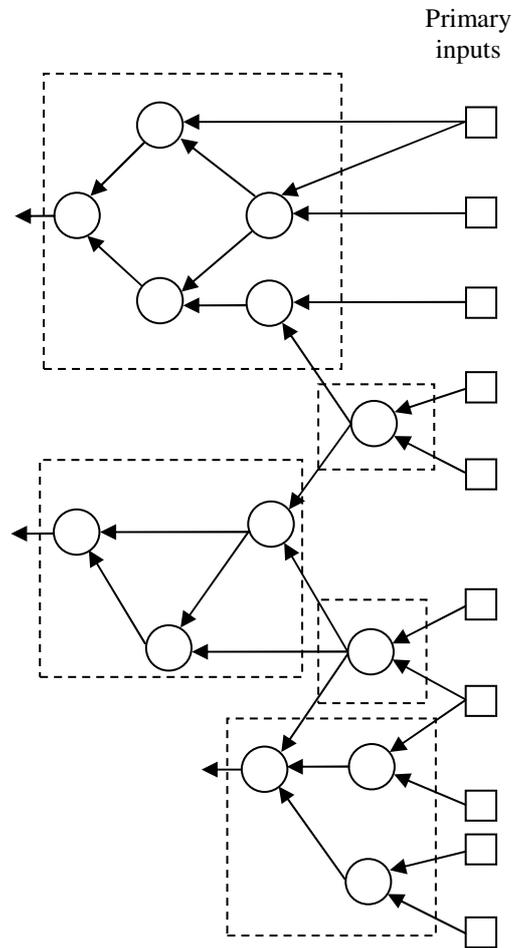
**Fig. 2.** Primary output lines and their transitive fan-in cones.

Figure 2 presents a generic circuit having multiple primary output (PO) lines. Each PO is tracing back towards primary inputs (PI) transitive fan-in cones (TFIC). These cones are, in general, non-disjoint (as one could remark in figure 2). Disjoint part of TFIC are named in [11] *Maximum Fanout Free Cone* (abbreviated MFFC). Nodes belonging to cone intersections are feeding multiple POs. Duplication free mapping proceeds over each MFFC. Restricting the mapping solution to be duplication free has benefits in terms of FPGA's routability (scarce resource). It was shown in [10] that any duplication-free mapping of node  $w$  is contained in the maximum fanout free cone of  $w$  (noted  $MFFC(w)$ ). It implies that best mapping for an arbitrary node  $w$  has to be searched in the set of all  $k$ -feasible cones rooted on  $w$  inside  $MFFC(w)$ .

Area minimization mapping of a circuit can be performed optimally by partitioning the circuit into a set of MFFCs and finding the optimal

mapping of each MFFC independently, in a separate approach (figure 3).

These results suggest a dynamic programming approach for duplication free mapping.



**Fig. 3.** MFFC partitioning network for duplication free mapping.

Given a network, for each node  $w$ , in topological order, is computed a level optimum and an area optimal of  $MFFC(w)$  is computed. When mapping of  $MFFC(w)$  is computed for each node  $u \in MFFC(w)$ ,  $u \neq w$ , an optimal mapping of  $MFFC(u)$  is already computed.

In this paper  $k$ -LUT mapping is made over *homogenous dominated cones*. It means that all nodes dominated only by  $z$ , or by  $z$  and  $t$ , as an example, will be mapped in a separate mapping process.

This strategy separates nodes having fan-outs in more than one single output cone and avoid interactions during mappings in different primary output cones. Additionally, this approach avoids multiple instances of nodes

having rich fan-outs in multiple transitive fanout cones.

Additionally, cones with multiple domination identification make simpler the task of mapping for critical performance.

Mapping phase starts by considering nodes that belongs to the set of critical paths. The primary output node  $z$  and all nodes belonging to the transitive cone rooted in this node define critical path, in figure 1.

Depending on the package's internal connection resources all non-critical path cones pending to the critical cone path could be duplicated and merged into the critical path cone, for speed.

Non-critical path pending cones will be merged into the critical one based on a linear criterion computed using graph quality factors (amount of internal nodes in such a non-critical cone, number of internal connections, minimal delay introduced etc).

However non-critical cones are considered in decreasing critical order and will be mapped separately and this will save area (CLBs) and internal interconnections resources.

Mapping process was implemented using *minDepth* algorithm as it was first described in [5] and *minLevelMapIII* algorithm derived from the previous one but with powerful additional heuristics as it was presented in [6], [7] and [8].

## 5. EXPERIMENTAL RESULTS

Implemented cluster algorithm working with *minLevelMapIII* (technological mapping) was tested against *minDepth* used without cluster partitioning.

Results are presented in Table 1.

Circuits, in Table 1 are taken from MCNC91 multilevel examples benchmark; being selected the most representative ones (as used in similar works).

Cone partitioning algorithm is similar to those previously presented in literature, [1], [5], [13], [15], [18], [19] and [30], but modified to minimize first critical path delay.

Heuristics introduced to evaluate cone's costs are based on the published results, [13], [16],

and [18], but them are slight modified because actual application was exclusively targeted to map  $k$ -LUT based FPGAs having primary goal to find best performance circuit and, after that, area optimal solution.

**Table 1:** Experimental results.

Circuit name	<i>minDepth</i>		<i>MinLevelMapIII with clustering</i>	
	depth	LUTcnt	depth	LUTcnt
<i>5xp1</i>	2	21	2	23
<i>9sym</i>	5	7	5	8
<i>C499</i>	4	67	4	72
<i>C5315</i>	8	500	8	543
<i>C880</i>	7	130	7	139
<i>alu2</i>	5	129	5	140
<i>alu4</i>	5	549	5	551
<i>apex2</i>	5	150	5	157
<i>apex4</i>	5	875	5	895
<i>apex6</i>	4	222	4	229
<i>apex7</i>	4	67	4	74
<i>b9</i>	3	37	3	41
<i>bw</i>	1	28	1	32
<i>clip</i>	3	44	3	47
<i>count</i>	3	74	3	76
<i>des</i>	5	1014	5	1080
<i>duke2</i>	4	151	4	158
<i>e64</i>	3	338	3	352
<i>f51m</i>	3	51	3	51
<i>misex1</i>	2	17	2	17
<i>misex2</i>	2	42	2	45
<i>rd73</i>	2	8	2	8
<i>rd84</i>	3	13	3	13
<i>rot</i>	6	204	6	227
<i>sao2</i>	4	57	4	57
<i>vg2</i>	3	35	3	35
<i>z4ml</i>	2	5	2	5

This was implemented by merging those clusters containing nodes belonging to the critical path but having enough *slack* in order to introduce no other costs to the partitioning objective.

Cluster generation, is based upon algorithm illustrated in [6] and provided most of the application's backgrounds.

Actual algorithm is computing all clusters *Clusters(n)* rooted on internal node  $n$  and having less inputs than  $M$  ( $M > \text{input}(\text{Clusters}(n))$ ) in an efficient way compared to the method *MaxFlow-MinCut* used in most of the non-heuristic existing works, see [8], [9], [10], [11], [24] and [13].

Comparing results for *minDepth* and *minLevelMapIII* it's obvious that almost all results are a little less adequate, in Table 1, for

*minLevelMapIII* (improved *minDepth*) with cluster partitioning.

That's because *minLevelMapIII* is working, mainly on the non-critical path cones, under the cone's boundaries and is not always able to find best merging nodes with this restriction, while *minDepth* is working ignoring cones boundary restrictions and finds always best area results (even using less sophisticated heuristics for that).

Although a number of clustering algorithms, such as the random walk based clustering algorithms [17] and [9], the clique based method [14], [16] and the multi-commodity-flow based method [32], have been developed most of them are not considering signal flow during cluster generation and finally cluster mapping.

#### 4. CONCLUSIONS AND FUTURE WORK

Existing cluster-based partitioning approaches have reported consistent improvements, in terms of both the cut size and the run time, over direct partitioning on the initial circuit.

Since fully automatic partitioning is essential for fast iterations in the design cycle, considerable effort is made in academia as well as in industry to facilitate and improve the difficult decisions on functional level.

Both mapping algorithms are, actually, under research and development in order to be able to accept various and complex *delay models* together with new mapping heuristics in order to obtain better *area* results.

Cluster partitioning algorithm, also under development, will be enhanced with new fast cost estimators making more efficient non-critical path cones process. Additional to the technological mapping of FPGA circuits, cluster-partitioning algorithm, has applications in large decision diagrams partitioning [7].

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