

FROM FORBIDDEN STATES TO LINEAR CONSTRAINTS FOR THE OPTIMAL SUPERVISORY SYNTHESIS

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Abstract: The place invariant method is well known as an elegant way to construct a Petri net controller. It is possible to use the constraint for preventing forbidden states. But in general case, there are many of the forbidden states, thus there is many control places. In this paper is presented a systematic method to reduce the size and the number of constraints. This method is applicable for safe and conservative Petri nets. By this method we can construct a maximally permissive controller.

Keywords: controller, Place invariant, Petri net, forbidden states, linear constraints.

1. INTRODUCTION

Petri Nets (PN) is a very appropriate and useful tool for the study of Discrete-Event Systems (DES) because of their modelling power and their mathematical properties. In the last decade, the research in the field of controller synthesis of DES became one of the most active domains [1], [3], [6].

In [4] and [11] a method for the optimal controller synthesis considering a safe PN was established. The method is based on the equivalence between the set of forbidden states and the set of linear constraints deduced from it. The use of the Yamalidou technique in [4] allows constructing a set of control places which represent the optimal controller. However the

number of control places is equal to the number of constraints and can become very important. Intuitively, we realized that the PN solution is not unique from the point of view of the structure, but the reachable space (graph of the markings) is naturally unique. The problem comes from all the linear constraints which can be simplified by holding structural properties of the PN. In this paper is proposed a systematic method of reduction of the number of constraints. The minimal solution is not unique in the general case, but a method to choose the best solution is presented. This approach is based on the hypothesis that the PN models are safe and conservative. This paper is organized as below:

In the second section will be presented the fundamental definitions then how we can construct the linear constraints from forbidden states. Later, in the fourth section, the method to reduce the number and the size of the constraints will be presented. At the end, this method will be explained through an example.

2. FUNDAMENTAL DEFINITIONS

In this paper it is supposed that reader knows the bases of the Petri net paradigm and we present only the notions used in this paper. For more details, see the book in [2]. A PN is presented by a 4-uplet $N = \{P, T, W, M_0\}$ where P is the set of places, T the set of transitions, W the incidence matrix and M_0 the initial marking. The graph of marking consists of nodes which correspond to the accessible markings, and of arcs to the firing of transitions. In this paper, we use the word state instead of marking, represented by all the marked places. In the graph of markings, there are three types of state: the authorized state, the forbidden state and the not reachable state. Among the forbidden states a particular and important subset is constituted by the border forbidden states, it is denoted by the set F . These states are such that all the input transitions are controllable.

In this paper, an important definition will be also used; it concerns the notion of over-state.

Definition 1: A state as $S_i = (P_{i1} \dots P_{in})$ is an over-state of $S_j = (P_{j1} \dots P_{jm})$ if $S_i \subseteq S_j$. $\square$

3. FROM FORBIDDEN STATES TO LINEAR CONSTRAINTS

The modelling approach presented in this paper, is the classic approach developed by Ramadge and Wonham ([9], [10]). The model of the process is synchronized with the specifications giving the closed loop desired functioning. The existence of uncontrollable transition often leads to the existence of forbidden states including the border forbidden states. They are systematically determined by using the Kumar algorithm [5]. We consider here that the PN models of both process and specifications are safe, but this does not mean that the marking of the control places is Boolean. Let f_i be a border forbidden state

from F and $\{P_{i1}P_{i2}P_{i3} \dots P_{in}\}$ be all the marked places which correspond to it. From the forbidden states¹, linear constraints can be constructed ([4], [11]). The linear constraint for the forbidden state f_i is given by Equation (1).

$$\sum_{k=1}^n m_{ik} = n - 1 \quad (1)$$

Where n is the number of marked place of f_i , and m_{ik} is the Boolean marking of place P_{ik} in state f_i . For example: If the state $(P_2P_5P_7)$ is a forbidden state, it can be avoided by using Equation (2)

$$m_2 + m_5 + m_7 = 2 \quad (2)$$

In this paper the forbidden state and its constraint is presented as below:

$$\begin{aligned} f_i &= \{P_{i1}P_{i2}P_{i3} \dots P_{in}\} \\ c_i &= \{P_{i1}P_{i2}P_{i3} \dots P_{in}, n-1\} \end{aligned} \quad (3)$$

The last term in c_i corresponds to the number of marked places in the forbidden state minus 1, it is called the bound. This is true only at the beginning.

4. REDUCTION OF THE SIZE AND NUMBER OF CONSTRAINTS

In real systems, the number of forbidden states can be very large. Knowing that for each forbidden state, one control place is added, the complexity of the controller can become unmanageable. For this reason, in this paper we propose a systematic method to reduce the size and the number of the constraints.

The PN models are assumed to be safe and conservative; then it is impossible for two places belonging to the same place invariant, to be marked simultaneously. This basic idea will be used for the simplification of the constraints.

Property 1: Let be $\{(P_1P_{i1} \dots P_{i(n-1)}), \dots, (P_r P_{i1} \dots P_{i(n-1)})\}$ r forbidden states in F .

$$m_1 + m_2 + \dots + m_r = 1 \quad (4)$$

The r constraints are equivalent to one constraint as below:

¹ Where there is no ambiguity, the word *border* will be omitted.

$$\begin{aligned}
m_1 + m_{i_1} + \dots + m_{i_{(n-1)}} &= n-1 \\
m_2 + m_{i_1} + \dots + m_{i_{(n-1)}} &= n-1 \\
&\dots \\
m_r + m_{i_1} + \dots + m_{i_{(n-1)}} &= n-1 \\
\iff \\
m_{i_1} + \dots + m_{i_{(n-1)}} &= n-2
\end{aligned}$$

Where n is the number of marked place.

Proof: necessary Condition:

The sum of all constraints gives the constraint follow:

$$(m_1 + m_{i_1} + \dots + m_{i_{(n-1)}}) + (m_2 + m_{i_1} + \dots + m_{i_{(n-1)}}) + \dots + (m_r + m_{i_1} + \dots + m_{i_{(n-1)}}) = r(n-1) \quad (5)$$

$$\begin{aligned}
(4), (5) &\Rightarrow \\
1 + r(m_{i_1} + \dots + m_{i_{(n-1)}}) &= r(n-1) \Rightarrow \\
m_{i_1} + \dots + m_{i_{(n-1)}} &= n-1-1/r \quad (m_i: \text{Integer number}) \Rightarrow \\
m_{i_1} + \dots + m_{i_{(n-1)}} &= n-2
\end{aligned}$$

Sufficient Condition:

$$\begin{aligned}
m_{i_1} + \dots + m_{i_{(n-1)}} &= n-2 \\
\forall k \in \{1, \dots, r\} \quad m_k = 1 &\Rightarrow m_k + m_{i_1} + \dots + m_{i_{(n-1)}} = \\
n-1
\end{aligned}$$

□

Let be $F = \{(P_1P_4P_7), (P_1P_4P_8), (P_1P_4P_9)\}$ set of a forbidden states and $m_7 + m_8 + m_9 = 1$, thus the over-state (P_1P_4) is forbidden state, without attention to marked place of the set $\{P_7, P_8, P_9\}$, or it is possible to use instead of three constraints only one constraint as below:

$$\begin{aligned}
m_1 + m_4 + m_7 &= 2 \\
m_1 + m_4 + m_8 &= 2 \xleftarrow{(m_7 + m_8 + m_9 = 1)} m_1 + m_4 = 1 \\
m_1 + m_4 + m_9 &= 2
\end{aligned}$$

Remark 1: it is possible to use property 1 more than one time.

□

For example, if the set F is as below:

$$F = \{(P_1P_4P_7P_{10}), (P_1P_4P_7P_{11}), (P_1P_4P_8P_{10}), (P_1P_4P_8P_{11}), (P_1P_4P_9P_{10}), (P_1P_4P_9P_{11})\}$$

and

$$\begin{aligned}
m_{10} + m_{11} &= 1 \\
m_7 + m_8 + m_9 &= 1
\end{aligned}$$

After the first use of Property 1 for the invariant between P_{10} and P_{11} the result is: $\{(P_1P_4P_7), (P_1P_4P_8), (P_1P_4P_9)\}$. Now it is possible to use

Property 1 for the other invariant. The final result will be the over-state (P_1P_4) .

Let us consider another set of forbidden states as below;

$$F' = \{(P_1P_4P_7P_{10}), (P_1P_4P_7P_{11}), (P_1P_4P_8P_{10}), (P_1P_4P_8P_{11})\}$$

At the end of first simplification the result is: $\{(P_1P_4P_7), (P_1P_4P_8)\}$ and it is not possible to use Property 1, but is it possible to reduce the number of constraint? The answer is yes. Because of the invariant between P_7, P_8 and P_9 , the states P_7 and P_8 cannot be marked in the same time. Thus both constraints can decrease in a constraint as below:

$$m_1 + m_4 + m_7 + m_8 = 2 \quad (6)$$

The property discussed above, is formalized in property 2:

Property 2: Let be $C = \{(P_1P_{i_1} \dots P_{i_{(n-1)}}, k), (P_2P_{i_1} \dots P_{i_{(n-1)}}, k), \dots, (P_rP_{i_1} \dots P_{i_{(n-1)}}, k)\}$ the equivalent constraints to forbidden states of marking graph and

$$m_1 + m_2 + \dots + m_r = 1 \quad (7)$$

The r constraints are equivalent to one constraint as below:

$$\begin{aligned}
m_1 + m_{i_1} + \dots + m_{i_{(n-1)}} &= k \\
m_2 + m_{i_1} + \dots + m_{i_{(n-1)}} &= k \\
&\dots \\
m_r + m_{i_1} + \dots + m_{i_{(n-1)}} &= k \\
\iff \\
m_1 + m_2 + \dots + m_r + m_{i_1} + \dots + m_{i_{(n-1)}} &= k
\end{aligned}$$

Where n is the number of marked place.

Proof: necessary Condition:

$$\begin{aligned}
\forall j \in \{1, \dots, r\} \quad m_j + m_{i_1} + \dots + m_{i_{(n-1)}} &= k \quad (8) \\
\text{and} \quad m_1 + m_2 + \dots + m_r &= 1
\end{aligned}$$

$\Rightarrow$

$$(m_1 + m_2 + \dots + m_r) + m_{i_1} + \dots + m_{i_{(n-1)}} = k+1$$

We are going to show that limit $k+1$ is never reached. If not, it is necessary that $m_1 + m_2 + \dots + m_r = 1$ and $m_{i_1} + \dots + m_{i_{(n-1)}} = k$. But if $m_{i_1} + \dots + m_{i_{(n-1)}} = k$, thus because of the constraints (8) it is necessary that for $\forall j \in$

$\{1, \dots, r\} \quad m_j = 0$. Then $m_1 + m_2 + \dots + m_r = 0$. Thus limit $k+1$ never is reached.

Sufficient Condition:

$$(m_1 + m_2 + \dots + m_r) + m_{i_1} + \dots + m_{i_{(n-1)}} = k$$

and $\forall i \in \{1, \dots, r\} \quad m_i = 0$

Then

$$\forall i \in \{1, \dots, r\} \quad m_i + m_{i_1} + \dots + m_{i_{(n-1)}} = k$$

□

Remark 2: While exploiting this property, constraints are used instead of states since the bound may change according to the simplifications.

□

4.1 Unreachable states

The objective of this approach is reduction the size and the numbers of the constraints. The final result is simpler if Property 1 is used. For this reason, our idea is to add the unreachable states in order to increase the space of forbidden states.

Definition 2: The unreachable states are the states that are not accessible from the initial state of the PN model or are reachable from border forbidden states.

□

If these states help to reduce constraints, it is possible to use these states as forbidden states. But at the end, it is not necessary to choose a constraint which does not covered any forbidden state. This will be explained later in Section 5.

4.2 Minimum of constraints

In order to have the minimum of constraints, it is necessary to choose the simplest constraints containing all the forbidden states. To reach this goal it is necessary to write all the final constraints with the forbidden states. A method similar with the one proposed by Mac Cluskey for the reduction of the logical expressions is used for determining the best choice [7]. Firstly, we must choose the simplified constraints which contain the forbidden states that are not in other constraints. Secondly for the forbidden states which are in two or several simplified constraints, it is needed to choose the constraint containing the greatest number of forbidden

states which were not chosen, or the constraint which is simpler. In generally, there is not only one answer. This will be more explained in the following section.

5. EXAMPLE

To illustrate the ideas developed in this paper, let us consider the example which was presented in [4]. A manufacturing system is composed of two independent machines $M1$ and $M2$, two transfer robots of the parts and one test bench where the final products are tested (Fig. 1).

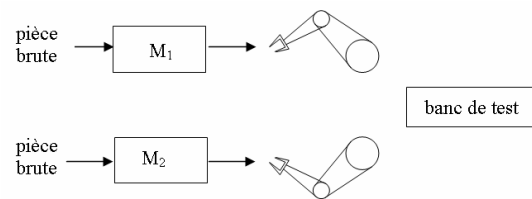


Fig. 1. Production line

Each machine has the following operating cycle: By occurrence of the event c_i , the machine starts working. When the work is finished (occurrence of event f_i) the produced part is transferred by the robot on the test bench, and a new cycle can be started again by occurrence of event t_i . There are two types of events in this system: the controllable events and uncontrollable events, only events c_1 and c_2 are controllable:

$$\hat{a}_c = \{c_1, c_2\} \text{ et } \hat{a}_u = \{f_1, t_1, f_2, t_2\}.$$

The model PN for this system is given in Fig. 2.

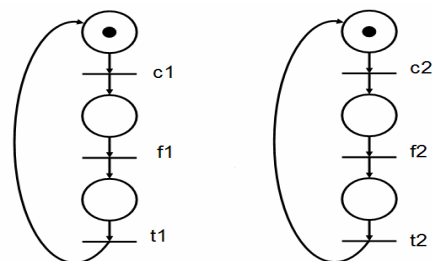


Fig. 2. PN process model.

The model of the specification of this system is presented in the Fig. 3. It is asked that firstly,

the robot transfers the product of machine M_1 and then the product of machine M_2 .

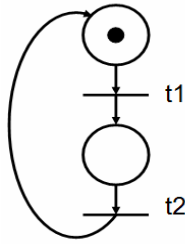


Fig. 3. PN specification model.

5.1 Desired functioning in closed loop

The determination of the forbidden states is made by the study of the controllability of the language of specification with regard to the language generated by the model of desired functioning in closed loop. In this example only transitions c_1 and c_2 are controllable and the other transitions are not controllable. The closed loop model of this system is illustrated in Fig. 4 and will be denoted as R_d . In this paper this model of PN is called Quasi-PN defined below.

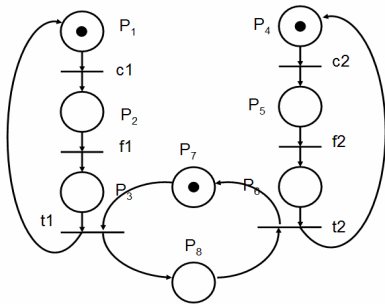


Fig. 4. Petri net model of closed loop system

Definition 3: A Quasi-PN is a PN which respects the following rules of firing:

- 1) A controllable transition is firable in the same way as in a classical PN.
- 2) An uncontrollable transition is firable if all its input places belonging to the process are marked

□

The difference of reachable markings between these two models (PN and Quasi—PN) indicates the forbidden states.

Definition 4: If in from a marking, an uncontrollable transition is firable for the

Quasi—PN model, but not for the real PN model, then this state is forbidden.

□

To determine the forbidden states by this method, it is necessary to construct the reachability graph for both models.

5.2 Reachability graph of the functioning closed loop

The reachability graph is an identification tool of the behaviour of the PN. A node in the reachability Graph represents the reachable markings, and arcs characterize the possible passages between these markings. A marking corresponds to a combination of marked places. There are 2^N possible states for a safe PN with N places. But for a conservative PN, the number of states is smaller. Thanks to the method presented in [2], the set of possible states can be calculated. The number of state is determined as below:

$$N = \prod_{i=1}^m (n_i) \quad (9)$$

Where n_i is the number of places in each marking invariant and m is the number of invariant.

From the reachability graph, the theory developed by Ramadge and Wonham allows to obtain the maximal permissive supervisor. If the language generated by the reachability graph is controllable, then the problem is resolved and the PN model R_d constitutes the controller. But if it is not controllable, it is necessary to determine all the forbidden states.

The reachability graph of the real – PN and quasi – PN are presented in Fig. 5 and 6. The comparison of the two graphs, gives the forbidden states.

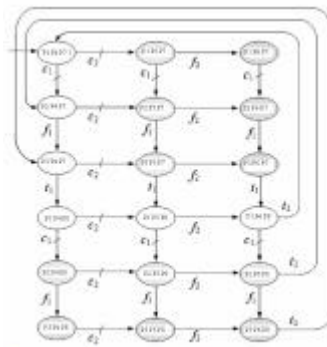


Fig. 5. Reachability graph of real - PN model R_d

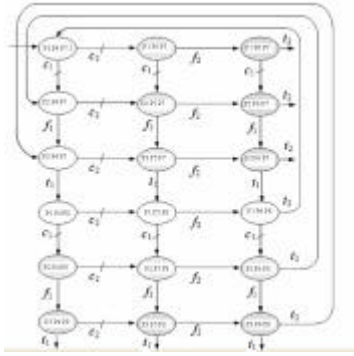


Fig. 6. Reachability graph of quasi – PN model R_4

By using Definition 3 it is possible to determine the set of forbidden states as below:

$$E = \{(P_7P_6P_1), (P_7P_6P_2), (P_7P_6P_3), (P_8P_4P_3), (P_8P_5P_3), (P_8P_6P_3)\} \quad (10)$$

From these states, weakly forbidden states are deduced. By the technique presented in [4], it is possible to find all the forbidden and weakly forbidden states that are called dangerous states. To prevent from reaching the dangerous states, it is sufficient to forbid the border states. All the input transitions of these states are controllable.

For the example, the border states are:

$$F = \{(P_7P_5P_1), (P_7P_5P_2), (P_7P_5P_3), (P_8P_4P_2), (P_8P_5P_2), (P_8P_6P_2)\} \quad (11)$$

From these 6 forbidden states, 6 constraints are deduced. We can now use the presented properties to reduce the size and the number of these constraints. For this, it is necessary to construct a set containing all the possible states and to indicate the type of each one.

In this example the marking invariants are obvious. For this example the number of possible states is calculated as below:

$$N = \prod_i^m (n_i) = 3 \cdot 3 \cdot 2 = 18 \quad (12)$$

5.3 Use of Properties 1 and 2

In this example there are three invariants and Property 1 is used for all.

States	S	States	S	States	S
$P_7P_4P_1$	1	$P_7P_4P_2$	1	$P_7P_4P_3$	1
$P_7P_5P_1$	0	$P_7P_5P_2$	0	$P_7P_5P_3$	0
$P_7P_6P_1$	?	$P_7P_6P_2$	?	$P_7P_6P_3$	?
$P_8P_4P_1$	1	$P_8P_4P_2$	0	$P_8P_4P_3$	?
$P_8P_5P_1$	1	$P_8P_5P_2$	0	$P_8P_5P_3$	?
$P_8P_6P_1$	1	$P_8P_6P_2$	0	$P_8P_6P_3$	?

1: admissible state 0: forbidden state ? : not reachable state

Fig. 7. All possible states

I: $m_1 + m_2 + m_3 = 1$:

Finding this invariant in Fig. 7 is easy, because in this case, all of the states are in one row. At the end it is obtained two over-states as below:

(P_5P_7) , it covers the states: $\{P_7P_5P_1, P_7P_5P_2, P_7P_5P_3\}$

(P_6P_7) , it covers the states: $\{P_7P_6P_1, P_7P_6P_2, P_7P_6P_3\}$

II? $m_4 + m_5 + m_6 = 1$:

By applying Property 1 for this invariant, the result is as below:

(P_8P_2) , covering $\{P_8P_4P_2, P_8P_5P_2, P_8P_6P_2\}$

(P_8P_3) , covering $\{P_8P_4P_3, P_8P_5P_3, P_8P_6P_3\}$

III? $m_7 + m_8 = 1$

(P_5P_2) , covering $\{P_7P_5P_2, P_8P_5P_2\}$

(P_6P_2) , covering $\{P_7P_6P_2, P_8P_6P_2\}$

(P_5P_3) , covering $\{P_7P_5P_3, P_8P_5P_3\}$

(P_6P_3) , covering $\{P_7P_6P_3, P_8P_6P_3\}$

The following table contains all the over states and indicates all the forbidden states which are covered by them. It may happen that a state is not covered, then it must be added in the final selection. It is not the case in this example (Fig. 8).

Over-states	The states which are covered	S
P_5P_7	$P_7P_5P_1, P_7P_5P_2, P_7P_5P_3$	0
P_6P_7	$P_7P_6P_1, P_7P_6P_2, P_7P_6P_3$	?
P_8P_2	$P_8P_4P_2, P_8P_5P_2, P_8P_6P_2$	0
P_8P_3	$P_8P_4P_3, P_8P_5P_3, P_8P_6P_3$	?
P_5P_2	$P_7P_5P_2, P_8P_5P_2$	0
P_6P_2	$P_7P_6P_2, P_8P_6P_2$	0
P_5P_3	$P_7P_5P_3, P_8P_5P_3$	0
P_6P_3	$P_7P_6P_3, P_8P_6P_3$	?

Fig. 8. All states after the first simplification

Here, Property 1 cannot be used longer, but in general case, it is possible to examine the table for new simplifications. Property 2 can now be used.

From now, we use the constraints instead of states or over-states since the bound may change according to the simplifications. There is two over-states or two constraint $\{(P_5P_7, 1), (P_6P_7, 1)\}$ which can be simplified by using Property 2. It is possible to use instead of two constraints only one constraint as bellow:

$$\{(P_5P_7, 1), (P_6P_7, 1)\} \Rightarrow (P_5 P_6P_7, 1) \quad (13)$$

The result after using Property 2 for all the constraints of Fig. 8 is illustrated in Fig. 9.

Constraint	The states which are covered	S
$P_5 P_6P_7, 1$	$P_7P_5P_1, P_7P_5P_2, P_7P_5P_3, P_7P_6P_1, P_7P_6P_2, P_7P_6P_3$	0
$P_8P_2 P_3,1$	$P_8P_4P_2, P_8P_5P_2, P_8P_6P_2, P_8P_4P_3, P_8P_5P_3, P_8P_6P_3$	0
$P_5 P_6P_2 P_3,1$	$P_7P_5P_2, P_8P_5P_2, P_7P_6P_2, P_8P_6P_2, P_7P_5P_3, P_8P_5P_3, P_7P_6P_3, P_8P_6P_3$	0

Fig. 9. All states after the last simplification

5.4 Minimum of constraint for this example

At the end of this level, it is necessary to choose the minimum and simplest constraints, containing all the forbidden states. In general case, it is possible to have some choice. The difference between two choices is the number of arc of the control places. The best choice is determined after the calculation of the control places.

At the end, the best solution contains two linear constraints (Fig. 10).

$$\begin{aligned} m_5+m_6+m_7 &= 1 \\ m_2+m_3+m_8 &= 1 \end{aligned} \quad (14)$$

	$P_7P_5P_1$	$P_7P_5P_2$	$P_7P_5P_3$	$P_8P_4P_2$	$P_8P_5P_2$	$P_8P_6P_2$	choice
$P_5 P_6P_7, 1$	v	v	v				v
$P_8P_2 P_3,1$				v	v	v	v
$P_5 P_6P_2 P_3,1$		v	v		v	v	
	v	v	v	v	v	v	

Fig. 10. Minimum of constraints

5.5 Calculation of control places

To calculate control places for every linear constraint, there is a systematic method given in [12]. The incidence matrix of the PN R_d , corresponding to the model of functioning in closed loop is W_p . The synthesis approach consists in adding to the incidence matrix W_p a matrix W_c corresponding to the control places. The incidence matrix of controlled system W will be constructed by adding a line to the matrix of incidence of controlled process W_p for every control place.

$$W = \begin{bmatrix} W_p \\ W_c \end{bmatrix} \quad (15)$$

It is then possible to calculate the matrix W_c and its initial marking as bellow:

$$W_c = -L.W_p \quad (16)$$

And

$$M_{cinit} = b - L.M_{pinit} \quad (17)$$

The controller is known by the determination of his matrix of incidence W_c and his initial marking M_{cinit} . By applying this result to the example, the result is:

$$W_c = \begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & -1 & 0 & 0 \end{bmatrix}$$

Fig. 11. The control matrix W_c

The initial marking of the control place is calculated:

$$\begin{aligned} m_{c1} &= 1; \\ m_{c2} &= 0; \end{aligned}$$

The PN of the final controller is represented in Fig.12.

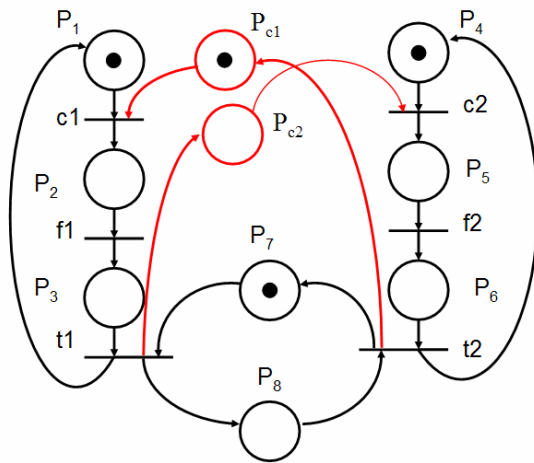


Fig. 12. Petri net model of closed loop system with control places

6. CONCLUSIONS

In this paper we have presented a systematic method to reduce the number of forbidden states or the number of equivalent linear constraints. The basic idea is to use the markings invariants of the PN to simplify these constraints. This is realized by using the not reachable states.

We obtain a structural solution easy to implement. The solution obtained by our approach gives the optimal controller. This optimality comes from the equivalence between all the admissible markings and all the linear constraints. The method that is presented in this paper is applicable for the systems modelled by Grafset if the place of control is safe.

Our future work consists in: 1) establishing complete algorithms and, 2) developing this approach for the system that is modelled by safe PN model not necessarily conservative.

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